## Confidence Interval & Confidence Sets

- 1. Define: (i) Confidence Interval, (ii) Length of the Confidence Interval, (iii) Shortest length of the Confidence Interval.
- 2. Define Confidence Sets. What are the types of Confidence Sets? Explain them very briefly.
- 3. What are the methods of constructing Confidence Sets? By inverting a normal test, explain the method of "Inverting a test statistics".
- 4. Explain the pivotal quantity along with an example.
- 5. Let  $X \sim N(\mu, \sigma^2)$ . Find the shortest length confidence interval for  $\mu$  by using pivotal quantity when,
  - (i)  $\sigma^2$  is known
  - (ii)  $\sigma^2$  is unknown
- 6. Let  $X \sim P(\theta)$  i.e.  $f(x; \theta) = \frac{e^{-\theta} \theta^x}{x!}$ ;  $x = 0,1,2,...,\infty$ . Find a  $100(1 \alpha)\%$  large sample C.I for  $\theta$  by using pivotal quantity.
- 7. Write down the properties of Confidence Sets. Distinguish between Confidence Sets and Confidence Interval. Illustrate the correspondance between Confidence Sets and Tests.
- 8. Define Simultaneous Confidence Interval. What are the methods of constructing Simultaneous Confidence Interval. Explain one of them.
- 9. Define Confidence Bands for Cumulative Distribution Functions with at least two examples.